

# Application of Credit Risk Management Model in Chinese Banks

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## Abstract

The main objective of this paper is to perform empirical analysis and research on the KMV and Zeta models, discussing whether banks in China could adopt both models in their credit risk management practices. In order to measure credit risk, the KMV model focuses on “Expected Default Probability” (EDP) that is calculated using Black-Scholes Option Pricing Formula. On the other hand, the Zeta Model focuses on determining the probability of a company going bankrupt two years prior to the event. Previous research on risk management has shown that the primary risk the banks generally face is credit risk as an increasingly greater number of banks suffer losses because of credit issues. This paper therefore aims to add to the existing literature a strong case for the relevance of both the KMV and Zeta models to be considered in the topic of banks’ credit risk management.

**Keywords:** KMV model, Zeta model, Expected default probability (EDP), Credit risk assessment

## 1. Introduction

### *1.1 Background*

Since the 1990s the global economic, political and technological landscapes have experienced a wide range of dramatic transformations, which have subsequently fueled an exponential growth in credit risk. And with the inception of a floating exchange rate regime, financial markets throughout the world have since witnessed an ongoing process of deregulation. While greater financial liquidity worldwide is creating opportunities for new capital sources to thrive, the increasing complexity of credit risk is posing a host of challenges.

In China, due to the current financial system in place, credit risk has inevitably become the main factor of financial risk—which is also influenced by:

- indirect financing that dominates the financial structure,
- precarious relationship between banks and enterprises,
- vague business distinction between bank policy and commerce,
- inadequate financial management,
- weak sense of risk,
- lack of effective internal mechanisms and risk prevention measures, and
- information asymmetry between borrowers and lenders, which could potentially lead to moral hazard.

On the evidence of the above, the financial risk situation in China reflects the more obvious characteristics of the traditional form of financial risk—as opposed to what is usually seen in other developed countries.

The credit risk faced by the commercial banks in China is largely affected by bad credit assets, tendency towards concentration of credit risk and insufficient credit risk management. So, measuring credit risk has become imperative to banks. The credit risk exposure featured in the New Basel Accord mainly involves five essential aspects, namely corporate risk, bank risk, retail risk, sovereign risk and equity risk— fully affirming the important role of IRB in risk management and capital regulation. The New Basel Accord proposes an IRB method for calculating credit risk, where the data analysis time period required for parameter estimation is long, and the source and content requirements are very high. Using the PD (probability of default), LGD (loss given default, which is amount of money a bank or other financial institution losses when a borrower defaults on a loan), EAD (exposure at default, which is the total value a bank is exposed to when a loan defaults) and M (maturity is the date on which the life of a transaction or financial instrument ends, after which it must either be reviewed.), we could ascertain the risk weight of different asset situations and then determine the risk assets.

As the credit risk management model gradually develops from being qualitative to being quantitative, both the KMV model and the Zeta model will be used to discuss the feasibility of applying a credit risk management model in China.

## 2. Literature Review

### 2.1 Literature Review

There are a number of research papers that revolve around credit risk management models, but for the purposes of our study, we shall focus our attention on those that discuss the KMV model and the Zeta model. Generally, the most common credit default model is the KMV model whereas the most accurate bankrupt probability model is the Zeta model.

Some scholars in China have researched the adaptability of KMV Model in China. Zhang Lin and Zhang Jialin (2000) as well as Wang Qiong and Chen Jinxian (2002) presented a theoretical comparison between the KMV model and the other models—pointing out that the KMV model might be more appropriate for the credit risk assessment of a public company. Xue Feng, Lu Wei, Zhao Heng Jie and Liu Jiyun (2003) used the data of China's stock market to determine the relationship function between the  $\sigma_E$  and  $\sigma_A$  in the actual equity market as they performed an empirical analysis based on a particular stock. Qiao Zhuo et al (2003) discussed the basic characteristics of the KMV model without any empirical evidence. On the other hand, Yi Danhui and Wu Jianmin (2004) calculated and compared the distance to default and default probability. With 30 companies in China randomly selected from the Shenzhen and Shanghai stock markets, the researchers verified the feasibility of measuring the listed company's credit risk by using distance to default.

According to Peter Crosbie (2003) the credit risk model can be summarized as follows. Credit risk can be divided into two components: single risk and portfolio risk. While single risk consists of PD, LGD and migration risk (Migration risk is a change in value caused by a deviation of the actual probability of a future default by an obligor from the expected probability of future default, adversely affecting the present value of the contract with the obligor today), portfolio risk comprises risk exposure and default correlations. In order to determine a company's credit risk default probability, we must calculate the company's value of assets, asset risk and leverage. As for the three-step method to calculate the expected default frequency of the KMV model, we must first estimate the market value of the company's assets and then calculate the volatility of those assets. And after we calculate the Distance to Default based on the volatility of the company's assets, we must eventually convert the Distance to Default to the expected default frequency using empirical distribution. As pointed out by Peter Crosbie (2003) the measurement of EDF is an effective tool in managing the credit process of institutions and continuous monitoring is the only way for detecting deterioration in credit quality. Because the EDF value is a real probability, it is widely used by institutions to measure credit risk.

Michel Crouhy, Dan Galai and Robert Mark (2000) performed a comprehensive analysis on the current credit risk models—comparing the CreditMetrics, KMV, CreditRisk+ and CreditPortfolioView models. CreditMetrics is a credit migration approach proposed by JP Morgan that accounts for the change of the company's credit quality within a time period. Meanwhile, the option pricing method or structural approach is initiated by KMV based on the asset value model originally proposed by Merton. KMV is then used to further develop the option pricing theory. As the endogenous default process in the model is compatible with the capital structure of the company, the company will suffer default when the asset value of the company is below a certain level. On the other hand, CreditRisk+ is an actuarial approach

proposed by Credit Suisse Financial Products (CSFP) to calculate default probability. Focusing on default probability using joint conditional distribution, this approach assumes that individual bonds and loans follow an exogenous Poisson process. As for the last model, Credit Portfolio View—proposed by McKinsey—is a time model using discrete time periods. Unlike the other models, Credit Portfolio View uses macroscopic variables—such as unemployment rate, government expenditure and GDP growth—that play a vital role in the credit cycle of the economy.

According to Michel Crouhy, Dan Galai and Robert Mark (2000) both the Credit Portfolio View and KMV methods are based on the same empirical observation, with their default risk and migration probability changing over time. While the KMV method adopts microeconomic factors by using the market value of assets to measure the PD of the debtor, the Credit Portfolio View method links the PD to the probability of mitigation by using macroeconomic factors. But we still need to calibrate default data for every country and corresponding industries. And the ad-hoc procedure in adjusting the mitigation matrix is another obvious limitation. Being more practical than the simple Bayesian model though, the proposed models should perform better because the revision of transition probability depends on the accumulation of internal professional knowledge of the bank's credit department and the internal credit quality assessment of a bank's given credit portfolio. The KMV method is related to the Credit Portfolio View method since the company's market value is mostly dependent on the economic situation. Therefore, the transition matrices produced by the KMV and Credit Portfolio View methods are comparable.

Edward I. Altman and Anthony Saunders (1998) summarized the development of credit risk models in the last two decades. First, the researchers discussed the evolution of individual loans and portfolio of the loans credit risk measurement put forward by the *Journal of Banking & Finance* and other well-known publications. Subsequently, the researchers presented a new mortality risk framework that could be used to measure the risk and return of loans and bonds. Offering us some hope for analyzing the risk-return structure of portfolio of debt instruments exposed to credit risk, the framework basically uses a variant Z-score model—called *Z'' – Score* model—to determine unexpected losses (the unexpected loss is the average total loss over and above the mean loss. It is calculated as a standard deviation from the mean at a certain confidence level. It is also referred to as Credit VaR.) and to assign a bond rating that is equivalent to the portfolio which each loan or bond may enter. As these scores and rating equivalents can consistently estimate expected losses, we should have a specific procedure for estimating unexpected losses if we have access to the standard deviation around the expected losses.

Edward I. Altman and Anthony Saunders (1998) also discussed the portfolio risk. The unexpected loss measure of  $UAL_p$  in the portfolio includes the correlation between the expected loss during the sample measurement period and the unexpected loss of personal assets. So, by comparing the bond rating equivalents, we can compute the expected value of the unexpected loss by using the standard deviation of the expected loss. It has also been highlighted that in order to gain the experience and confidence in applying this fixed income portfolio technology, we must spend more time in studying additional samples.

Stephen Kealhofer and Matthew Kurbat (2002) discussed the use of Merton's method to predict default based on debt ratings and accounting variables. Adding Moody's rating and accounting variables into Merton's method can significantly improve the viability of default prediction. It is important to note that both the Moody's ratings and the accounting variables contain default prediction information that is beyond the predictive information presented in Merton's method. However, it is still possible to show all default predictive information of Moody's ratings and accounting variables in the KMV expected default frequencies. With less incorrect default identification that is observed in other models, the expected default frequencies of KMV are more uniform. It is also worth noting that Merton's approach generally performs better than Moody's credit rating or other accounting ratios in forecasting default conditions—due to the stronger connection that Merton's approach has with accounting variables. To predict future share price, Merton's method uses historical share price information that includes information ratios such as return on asset and returns on equity. It has also been pointed out that the Merton's approach is unfair, due to the various judgements made about non-defaulting companies. Every method faces the possibility of generating too many false rejections, but this is hardly surprising since ratings and accounting ratios cannot be fully projected in the share price. There are just too many factors affecting the share price.

### **3. Research Methodology**

#### *3.1 KMV Model Overview*

The original intention of KMV Corporation in creating the KMV model was to estimate the default probability of KMV company's borrowers. The KMV model has two stages. The first stage of the KMV model is to test the precision of the model by comparing the predicted results with the actual results. It has been observed that in most cases the KMV model can truly reflect the size of credit risk, thanks to a high sensitivity to credit risk. The second stage of KMV model is to verify the validity of the model—a subject that many famous scholars have studied before.

The pricing basis of the KMV model is modern option pricing theory, which has been a major innovation in the measurement of credit default. The KMV model has several advantages. Besides fully utilizing the information available in the capital market, the KMV model can be used to quantitatively analyze the credit risk of listed companies. Since the data used by the KMV model is derived from stock price information of listed companies rather than internal data that is generated within the company itself, the company's current credit situation can be accurately projected. In addition, the KMV model is based on a number of previous theories—such as corporate finance theory and option pricing theory—so there is a theoretical basis to support its viability.

The KMV model is more suitable for credit quality evaluation of listed companies because listed companies are more transparent about their data whereas the data of non-listed companies is less accessible. When we apply the KMV model to non-listed companies, we need to adjust the parameters of the model. And because the expected default probability is the result of comparative analysis, the accuracy of the model may be somewhat compromised. Most importantly, the KMV model assumes that the value of company assets conforms to the

characteristics of lognormal distribution, but the value of company assets generally exhibits non-normal statistical characteristics in reality.

In short, the KMV model offers certain practical significance in calculating the probability of default.

### *3.2 Zeta Model Overview*

Derived from quantitative and qualitative methods, the scoring model is a statistical method which uses a large amount of historical data to determine parameters and predict variables of default probability. LDA (Linear discriminant analysis: it is a generalization of Fisher's linear discriminant, a method used in statistics, pattern recognition and machine learning to find a linear combination of features that characterizes or separates two or more classes of objects or events. ) is one of the most commonly used statistical methods in developing scoring models. Generally, due to the choice of exogenous variables, default composition and default definition, usage of the LDA-based model is reduced. An LDA produces a scoring function, which is a linear function of variables. These variables are chosen based on their estimated contribution to the likelihood of default, the large number of qualitative characteristics and the accounting ratios. Each accounting ratio could have a big or small impact on the overall score, as determined by Altman's Z-score. Although there are many ways to calculate Z-score, the most commonly used method is the least squares method.

Proposed by Edward I. Altman, an Assistant Professor of Finance at New York University in 1968, Z-score is a quantitative analysis method used to determine the condition of the balance sheet. The lower the Z-score, the greater the probability for the company to face a financial problem in the future under normal circumstances. LDA divides the companies into two groups: performing or solvent companies and defaulting or insolvent companies. One of the challenges of such classification is whether or not we can predict which companies will be solvent and which companies will be insolvent before default. Although the approach is flawed as both solvent and insolvent companies may have similar scores, the Z cut-off point is used to distinguish the two groups.

Altman's Z-score is also used to estimate the possibility of financial distress, which is denoted by a weighted average of five financial ratios. As sharp decline in the company's share price is mostly caused by balance sheet issues, financial statements have a strong influence on shareholders' judgement of the company. The importance of financial ratios is therefore self-evident.

Altman's initial research was based on financial data from manufacturing companies. Focusing on 66 companies where half had applied for bankruptcy, Altman calculated various financial indicators for those 66 companies, obtained their corresponding weights through discrete methods and selected the most important weights to build the relevant model. To validate the model, Altman calculated the Z-score for groups of bankrupt and non-bankrupt but sick companies, i.e. ST companies. Altman's goal was to ascertain how well the model could distinguish between sick companies and those that had gone bankrupt.

It was observed that Altman's model predicted with a 72% accuracy a company's bankruptcy two years in advance. In the next 31 years of testing though, it was discovered that the accuracy of the model in predicting bankruptcy one year in advance had eventually increased to 80%–90%. Using the Z-score to rank a group of European companies in 2009, Graham Secker—a Morgan Stanley strategy analyst—found that companies with weaker balance sheets underperformed in most cases as those with a Z score of less than 1 usually underperformed by more than 4%.

If the company is not listed, the market value of the company cannot be obtained directly. The Zeta model therefore has different forms for listed companies and non-listed companies. When the company is listed, the Z-score is calculated as follows:

$$Z = 1.2X_1 + 1.4X_2 + 3.3X_3 + 0.6X_4 + 1.0X_5$$

where

Z: the overall index of the Z-score model

$X_1$ : working capital / total assets

This suggests the company may experience shrinking liquidity when the company's liquid assets double.

$X_2$ : retained earnings / total assets

This ratio measures profitability, which reflects the company's age and earning power.

$X_3$ : earnings before interest and tax / total assets

This ratio shows the efficiency of the company in generating earnings under the same asset size.

$X_4$ : market value of equity / book value of total liabilities

This ratio provides a quick test of how much the company's assets can fall before the company becomes technically insolvent, i.e. when its liabilities exceed its assets.

$X_5$ : sales / total assets

This ratio represents asset turnover, which measures how effectively the company uses its assets to generate sales.

A great deal of factual research has shown that investors must do some serious due diligence before considering whether to invest in a company with an Altman Z-score of close to or less than 3. Companies can be classified according to their Z-score as follows:

- When the company's Z-score is more than 2.99, based on the financial figures only, the company is placed in the "Safe" zone.
- When the company's Z-score ranges from 1.80 to 2.99, based on the financial figures only, the company is placed in the "Grey" zone. The company may or may not go bankrupt in the next two years.

- When the company's Z-score is less than 1.80, based on the financial figures only, the company is placed in the “Distress” zone. There is a high probability that the company will face distress in the next two years.

When the company is not listed, the Z-score is calculated as follows:

$$Z_1 = 0.717X_1 + 0.847X_2 + 3.107X_3 + 0.42X_4 + 0.998X_5$$

where

Z: the overall index of the Z-score model for private manufacturing companies

$X_1$ : working capital / total assets

This suggests the company may experience shrinking liquidity when the company's liquid assets double.

$X_2$ : retained earnings / total assets

This ratio measures profitability that reflects the company's age and earning power.

$X_3$ : earnings before interest and tax / total assets

This ratio shows the efficiency of the company in generating earnings under the same asset size.

$X_4$ : book value of equity / total liabilities

This formula uses the book value of equity, not the market value of equity.

$X_5$ : sales / total assets

This ratio represents asset turnover, which measures how effectively the company uses its assets to generate sales.

Non-listed companies can be classified according to their Z-score as follows:

- When the company's Z-score is more than 2.9, based on the financial figures only, the company is placed in the “Safe” zone.
- When the company's Z-score ranges from 1.23 to 2.9, based on the financial figures only, the company is placed in the “Grey” zone. The company may or may not go bankrupt in the next two years.
- When the company's Z-score is less than 1.23, based on the financial figures only, the company is placed in the “Distress” zone. There is a high probability that the company will face distress in the next two years.

Asset turnover changes according to the industry the company is in. Since the above formula is mainly used for companies in the manufacturing industry, we need to consider the following Altman models that provide corresponding formulas for non-manufacturing companies.

For non-manufacturing companies, the Z-score is calculated as follows:



$$Z_2 = 6.56X_1 + 3.26X_2 + 6.72X_3 + 1.05X_4$$

where

Z: the overall index of the Z-score model for private manufacturing companies

$X_1$ : working capital / total assets

This suggests the company may experience shrinking liquidity when the company's liquid assets double.

$X_2$ : retained earnings / total assets

This ratio measures profitability that reflects the company's age and earning power.

$X_3$ : earnings before interest and tax / total assets

This ratio shows the efficiency of the company in generating earnings under the same asset size.

$X_4$ : book value of equity / total liabilities

This formula uses the book value of equity, not the market value of equity.

Non-manufacturing companies can be classified according to their Z-score as follows:

- When the company's Z-score is more than 2.6, based on the financial figures only, the company is placed in the "Safe" zone.
- When the company's Z-score ranges from 1.1 to 2.6, based on the financial figures only, the company is placed in the "Grey" zone. The company may or may not go bankrupt in the next two years.
- When the company's Z-score is less than 1.1, based on the financial figures only, the company is placed in the "Distress" zone. There is a high probability that the company will face distress in the next two years.

### 3.3 Data Acquisition

Since information on the bad credit records of listed companies is not disclosed publicly, we must use other means to ascertain the default probability of these companies. One way of computing the default probability is to calculate the stock yield using information on the stock price of the listed companies and then determine the default distance.

30 listed companies have been randomly selected from China's Shanghai and Shenzhen stock markets. The financial data of these companies from 1 January 2017 to 31 December 2017 is shown in Table 1. There are 10 listed companies with good performance, 10 listed companies with mediocre performance and 10 listed companies with poor performance. Through the following analysis, the feasibility of the KMV and Zeta models in reality can be ascertained.

According to the empirical analysis of a large number of default events, it has been highlighted by the KMV model that:

- when the long-term debt value is less than 1.5 times the short-term debt value, the most frequent default critical point is located near the company's short-term debt value plus 0.5 times the long-term debt value, but
- when the long-term debt value is more than 1.5 times the short-term debt value, the most frequent default critical point is located near the company's 0.7 times total of short-term debt value and long-term debt value.

There are some basic assumptions in this paper.

- The default distance formula that defines the company's market value is larger than its debt value in a year, assuming that the growth rate of the company's asset value is zero.
- The stock price of a company is consistent with logarithmic normal distribution and the stock price volatility is derived from stock price logarithmically.
- The annual volatility of equity is computed using the stock closing price of the 252 trading days in 2017.
- The annual risk-free interest rate is fixed. The standard one-year maturity yield of China's treasury bond in 2017 and  $r = 2.7484\%$  are used.
- Equity is a call option on the firm value with a strike price that is equal to the face value of debt.

Table 1. 30 Listed Companies from Shanghai and Shenzhen Stock Markets

<b>Blue-chip Companies (Note 1)</b>		<b>Ordinary Companies (Note 2)</b>	
<b>Code</b>	<b>Industry</b>	<b>Code</b>	<b>Industry</b>
600519	Wine & Beverage	600000	Banking
002302	Metal & Nonmetal	000905	Transportation
300176	Machinery & Equipment & Instrument	600549	Metal & Nonmetal
002307	Construction Business	603377	Transportation
002081	Decoration	600479	Pharmaceuticals
600808	Metal & Nonmetal	002403	Metal & Nonmetal
000709	Metal & Nonmetal	600826	Business Brokerage & Agency
601919	Marine Traffic	300220	Electronics
601899	Nonferrous Metal Mining	300104	Information Dissemination Service
600340	Real Estate Development	600363	Electronics
<b>ST Companies (Note 3)</b>		<b>ST Companies</b>	
<b>Code</b>	<b>Industry</b>	<b>Code</b>	<b>Industry</b>
600860	Machinery & Equipment & Instrument	600608	Metal & Nonmetal
002490	Machinery & Equipment & Instrument	600403	Coal Mining
000526	Real Estate Development	601005	Metal & Nonmetal
600696	Real Estate Development	000932	Metal & Nonmetal
000595	Machinery & Equipment & Instrument	000982	Textile & Clothing &Fur

Note 1. Blue-ship Companies: They are the mature companies in the stock market that represent the stalwarts of industry-safe, stable, profitable, and long-lasting companies that represent relatively safe, low volatility investments.

Note 2. Ordinary Companies: The companies with mediocre performance.

Note 3. ST Companies: ST stand for special treatment. Under regulation of Shenzhen Stock Exchange and Shanghai Stock Exchange, in the event of financial issues or other abnormal conditions of listed companies that make investors unable to judge the future of the companies and may endanger the interest of investors, the Stock Exchange shall take special treatment on these stocks.

#### 4. Calculation and Results

##### 4.1 The Calculation and Results

##### Equity Value Volatility ( $\sigma_E$ )

In this paper, the volatility of equity value is derived from historical stock price data. Assuming that the stock price of listed companies conforms with logarithmic normal distribution, the volatility of equity value is expressed as:

$$\delta_i = \ln\left(\frac{S_i}{S_{i-1}}\right)$$
$$\sigma_E = \frac{\sqrt{\frac{1}{n-1} \sum_{i=1}^n \delta_i^2 - \frac{1}{n(n-1) (\sum_{i=1}^n \delta_i)^2}}}{\sqrt{\frac{1}{n}}}$$

where

$S_{i-1}, S_i$ : the stock closing price on day  $i$  and  $i - 1$

$n$ : the trading day, where 252 days have been selected as the benchmark

$\delta_i$ : the log return at time  $i$

$\sigma_E$ : the annual volatility of equity value

The results, including the volatility of equity value computed using Microsoft Excel, are shown in Table 2.

Table 2. Average Return and Annual Equity Volatility of Selected Companies

Blue-chip Stock			Common Stock		
Code	Average Return*	Annual Equity Volatility	Code	Average Return*	Annual Equity Volatility
600519	0.3010%	0.2026	600000	-0.1063%	0.2302
002302	0.3453%	0.6604	000905	0.0059%	0.4636
300176	0.5908%	0.5288	600549	0.0639%	0.4549
002307	0.1180%	0.6060	603377	0.0006%	0.2424
002081	0.1805%	0.2988	600479	-0.0466%	0.2272
600808	0.1512%	0.3902	002403	-0.0738%	0.2005
000709	0.0650%	0.4288	600826	-0.3042%	0.3112
601919	0.1023%	0.3495	300220	-0.1605%	0.4474
601899	0.1284%	0.2531	300104	-0.3490%	0.7298
600340	0.1124%	0.3755	600363	-0.1158%	0.3480
ST Stock			ST Stock		
Code	Average Return (Note 1)	Annual Equity Volatility	Code	Average Return*	Annual Equity Volatility
600860	-0.2184%	0.3106	600608	-0.2975%	0.3795
002490	-0.2840%	0.3850	600403	-0.0819%	0.1850
000526	-0.0336%	0.2347	601005	-0.0653%	0.1994
600696	-0.2577%	0.3426	000932	0.1206%	0.4118
000595	-0.2903%	0.4744	000982	-0.3955%	0.3613

Note 1. Average Return: It means daily average return.

**DPT** (Default point is the level of the market value of a company's assets, below which the firm would fail to make scheduled debt payments. The default point is firm specific and is a function of the firm's liability structure.)

According to the 2017 annual report of the selected listed companies, DPT can be derived from year-end short-term liabilities and long-term liabilities. Existing companies use a variety of debt instruments (with different maturities, coupons and so forth) so there is no unique DPT.

“Purely empirical” rule of thumb (De Servigny/ Renault [2004] and KMV [2002]) where STD is short term debt and LTD is long term debt:

$$\text{Default Point} = \begin{cases} STD + 0.5LTD & \text{if } LTD/STD < 1.5 \\ STD + \left(0.7 - \frac{0.3STD}{LTD}\right) * LTD & \text{otherwise} \end{cases}$$

The results are shown in Table 3.

Table 3. DPT of Selected Companies

<b>Blue-chip Stock</b>			
<b>Code</b>	<b>Short-term Debt (Million)</b>	<b>Long-term Debt (Million)</b>	<b>DPT (Million)</b>
600519	38,574.92	15.57	38,582.70
002302	9,489.41	2,023.70	10,501.26
300176	1,349.78	191.77	1,445.67
002307	10,844.23	5,439.59	13,564.02
002081	16,022.89	411.32	16,228.55
600808	28,093.36	10,324.06	33,255.39
000709	113,240.57	29,248.25	127,864.70
601919	43,491.99	45,987.43	66,485.71
601899	28,793.59	22,878.83	40,233.01
600340	228,063.69	76,768.47	266,447.92
<b>Common Stock</b>			
<b>Code</b>	<b>Short-term Debt (Million)</b>	<b>Long-term Debt (Million)</b>	<b>DPT (Million)</b>
000905	2,974.20	1,578.95	3,763.68
600549	8,200.72	1,902.12	9,151.78
603377	709.74	256.82	838.15
600479	934.39	111.33	990.05

002403	1,530.95	562.85	1,812.38
600826	958.60	332.15	1,124.68
300220	99.56	1.31	100.21
300104	14,494.25	4,069.89	16,529.19
600363	1,682.18	66.09	1,715.23
<b>ST Stock</b>			
<b>Code</b>	<b>Short-term Debt (Million)</b>	<b>Long-term Debt (Million)</b>	<b>DPT (Million)</b>
002490	3,531.93	759.54	3,911.70
000526	3,501.99	17.64	3,510.81
600696	501.90	16.58	510.19
000595	883.89	225.15	996.47
600608	121.21	4.75	123.59
600403	8,595.46	846.06	9,018.49
601005	4,810.95	3,397.55	6,509.72
000932	47,920.36	12,428.63	54,134.67
000982	8,469.57	1,773.63	9,356.39

### Asset Value Volatility ( $\sigma_A$ )

The KMV model assumes that when the asset value of a company is less than the value of its liabilities, the company will default. We can get the market value and volatility of assets through the Black-Scholes-Merton (BSM) options pricing method. The model also assumes that the company's capital structure contains only equity and short-term debt, which are recognized as cash or cash equivalents. Long-term debt is considered permanent and can be converted into preferred stock. Having made the above basic assumptions, we can use recursion based on the following formula to find out the asset value volatility:

$$E = V * N(d_1) - D * e^{-r(T-t)} * N(d_2)$$

$$d_1 = \frac{\ln \frac{V}{D * e^{-r(T-t)}}}{\sigma_A * \sqrt{T-t}} + \frac{1}{2} \sigma_A * \sqrt{T-t}$$

$$d_2 = d_1 - \sigma_A * \sqrt{T-t}$$

$$N(d) = \int_{-\infty}^d \frac{1}{\sqrt{2\pi}} e^{-\frac{1}{2}x^2} dx$$

The relationship between volatility of the underlying asset value ( $\sigma_A$ ) and the volatility of the equity market value ( $\sigma_E$ ) is as follows:

$$\sigma_E = N(d_1) * \left(\frac{V_t}{E_t}\right) * \sigma_A$$

$$\text{DefaultProbability} = 1 - N(d_2) = N(-d_2)$$

where

V: market value of the asset

D: face value of the company's zero-coupon debt maturing at T (only liability)

$\sigma_A$ : the standard deviation of the assets value

$\sigma_E$ : the standard deviation of the equity value

r: the risk-free interest rate

$N(d)$ : cumulative normal distribution function evaluated at d

$T - t$ : the time interval (maturity)

Using Microsoft Excel, the equations are solved via the iterative method. The asset value volatility has been calculated and the results are shown in Table 4.

Table 4. Default Probability of Selected Companies

<b>Blue-chip Stock</b>					
<b>Code</b>	<b>Market Value Assets (Million)</b>	<b>Asset Volatility</b>	$d_1$	$d_2$	<b>Default Probability</b>
600519	914,768.11	0.1941	16.5527	16.3586	1.888E-60
002302	32,617.70	0.4478	2.8161	2.3683	0.0089344
300176	15,402.80	0.4792	5.2347	4.7556	9.894E-07
002307	19,913.22	0.1932	2.2260	2.0328	0.0210386
002081	56,724.04	0.2133	6.1026	5.8893	1.939E-09
600808	65,059.21	0.1908	3.7574	3.5667	0.0001808
000709	169,277.27	0.1049	2.9891	2.8842	0.0019622
601919	135,649.89	0.1782	4.2445	4.0663	2.388E-05
601899	50,804.34	0.0527	4.9771	4.9244	4.231E-07



600340	359,203.70	0.0970	3.4128	3.3158	0.0004569
<b>Common Stock</b>					
<b>Code</b>	<b>Market Value Assets (Million)</b>	<b>Asset Volatility</b>	$d_1$	$d_2$	<b>Default Probability</b>
600000	5,258,054.19	0.0162	6.2116	6.1955	2.906E-10
000905	9,360.42	0.2772	3.5249	3.2478	0.0005816
600549	37,121.61	0.3427	4.3370	3.9943	3.244E-05
603377	17,629.75	0.2309	13.4270	13.1961	4.618E-40
600479	5,879.61	0.1890	9.6679	9.4790	1.284E-21
002403	6,145.85	0.1414	8.9007	8.7593	9.824E-19
600826	6,664.54	0.2587	7.1146	6.8560	3.542E-12
300220	2,639.11	0.4305	7.8778	7.4473	4.762E-14
300104	77,687.31	0.5745	3.0287	2.4542	0.0070603
600363	7,285.30	0.2661	5.6716	5.4055	3.231E-08
<b>ST Stock</b>					
<b>Code</b>	<b>Market Value Assets (Million)</b>	<b>Asset Volatility</b>	$d_1$	$d_2$	<b>Default Probability</b>
600860	3,725.82	0.2416	6.465176	6.223527	2.431E-10
002490	7,829.14	0.1926	3.841322	3.648702	0.0001318
000526	7,039.24	0.1176	6.206955	6.089336	5.669E-10
600696	2,505.90	0.2728	6.071256	5.798442	3.347E-09
000595	4,978.31	0.3794	4.50202	4.122615	1.873E-05
600608	2,728.17	0.3624	8.796849	8.434495	1.663E-17
600403	20,207.49	0.1025	8.194313	8.091863	2.938E-16
601005	25,684.72	0.1488	9.481618	9.332787	5.156E-21
000932	78,591.60	0.1281	3.187562	3.059412	0.0011089
000982	15,674.04	0.1456	3.80494	3.659331	0.0001264

### Recovery Rate ( $\rho_t$ ), Expected Loss Given Default (LGD)

According to Merton's model, at the default point of the face value of the debt, the distance to default can be calculated using the volatility of the company's assets. When the computed "Distance to Default" is high, the company is less likely to default. Since the asset value

volatility has already been computed, the aim here is to calculate the Distance to Default in order to determine the probability of default. The following formula is used:

$$Distance\ Default(DD) = \frac{V_t - DPT}{\sigma_A V_t}$$

where

$V_t$ : the market value of the company's assets

$\sigma_A$ : the standard deviation of the asset value

The Merton model for LGD assumes that the company's value is lognormal distributed with a constant volatility and the company only has one liability, which is zero-coupon debt issue. The formula is as follows:

$$Recovery\ Given\ Default\ (RGD_t) = V_t * N(-d_1)/N(-d_2)$$

$$Recovery\ Rate\ (\rho_t) = RGD_t/D$$

$$Expected\ Loss\ Given\ Default\ (LGD_t) = e^{-rt} * D - RGD_t$$

where

$V_t$ : the market value of the company's assets at time t

$D$ : the face value of the company's zero-coupon debt maturing at T (only liability)

$r$ : the expected return on the value of the company, which uses risk-free interest rates

Using Microsoft Excel, the recovery rate, recovery given default and expected loss given default are computed. The results are shown in Table 5.

Table 5. Distance to Default and Expected Loss Given

Default of Selected Companies

<b>Blue-chip Stock</b>				
<b>Code</b>	<b>Distance to Default</b>	<b>Recovery Given Default (Million)</b>	<b>Recovery Rate</b>	<b>Expected Loss Given Default (Million)</b>
600519	4.9358	37,099.84	96.1567%	37,536.74
002302	1.5141	8,872.21	84.4871%	10,216.57
300176	1.8911	1,286.08	88.9608%	1,406.48
002307	1.6501	12,311.94	90.7691%	13,196.30
002081	3.3470	15,263.45	94.0531%	15,788.60
600808	2.5626	30,891.31	92.8911%	32,353.85
000709	2.3322	120,700.76	94.3973%	124,398.32

601919	2.8609	62,211.96	93.5719%	64,683.30
601899	3.9503	38,756.33	96.3297%	39,142.30
600340	2.6633	252,787.43	94.8731%	259,224.59
<b>Common Stock</b>				
<b>Code</b>	<b>Distance to Default</b>	<b>Recovery Given Default (Million)</b>	<b>Recovery Rate</b>	<b>Expected Loss Given Default (Million)</b>
600000	4.3444	4,744,171.22	97.0474%	4,755,985.17
000905	2.1573	3,408.85	90.5725%	3,661.64
600549	2.1984	8,262.13	90.2789%	8,903.68
603377	4.1250	801.56	95.6342%	815.43
600479	4.4011	944.77	95.4266%	963.21
002403	4.9864	1,735.90	95.7804%	1,763.24
600826	3.2137	1,055.87	93.8818%	1,094.19
300220	2.2349	92.33	92.1360%	97.50
300104	1.3702	13,512.09	81.7468%	16,081.09
600363	2.8733	1,594.77	92.9770%	1,668.73
<b>ST Stock</b>				
<b>Code</b>	<b>Distance to Default</b>	<b>Recovery Given Default (Million)</b>	<b>Recovery Rate</b>	<b>Expected Loss Given Default (Million)</b>
600860	3.2200	775.52	93.8114%	804.27
002490	2.5977	3,635.02	92.9270%	3,805.65
000526	4.2617	3,353.92	95.5313%	3,415.63
600696	2.9192	475.15	93.1316%	496.36
000595	2.1081	894.55	89.7720%	969.45
600608	2.6347	115.41	93.3809%	120.24
600403	5.4046	8,667.37	96.1066%	8,774.00
601005	5.0161	6,235.95	95.7944%	6,333.24
000932	2.4283	50,845.72	93.9245%	52,667.10
000982	2.7681	8,791.66	93.9643%	9,102.74

#### 4.2 Zeta Model Empirical Analysis

The companies we choose are listed companies, so the Z-score is calculated as follows:

$$Z = 1.2X_1 + 1.4X_2 + 3.3X_3 + 0.6X_4 + 1.0X_5$$

We use this formula to calculate the results, which are shown in Table 6.

Table 6. Zeta Value of Selected Companies

<b>Blue-chip Companies</b>						
Code	T1	T2	T3	T4	T5	Zeta
600519	0.5473	0.6554	0.2893	32.4543	0.4536	22.4552
002302	0.3020	0.1224	0.0113	1.9210	0.8187	2.5422
300176	0.0740	0.2570	0.2456	9.0539	1.1087	7.8001
002307	0.0386	0.0222	0.0065	0.3899	0.5024	0.8350
002081	0.2895	0.3077	0.0829	2.4641	0.7450	3.2750
600808	-0.0557	0.1073	0.0783	0.7075	1.0144	1.7804
000709	-0.3208	0.0626	0.0163	0.2906	0.5731	0.5040
601919	-0.0304	-0.1180	0.0372	0.7730	0.6792	1.0641
601899	-0.0013	0.2409	0.0563	0.2046	1.0586	1.7027
600340	0.3204	0.0577	0.0343	0.3043	0.1587	0.9196
<b>Ordinary Companies</b>						
Code	T1	T2	T3	T4	T5	Zeta
600000	-0.0092	0.0349	0.0115	0.0648	0.0275	0.1418
000905	-0.0666	0.2626	0.0289	1.2292	1.6965	2.8172
600549	0.0818	0.1282	0.0641	2.7685	0.7527	2.9028
603377	0.0848	0.1782	0.1043	17.3725	0.3713	11.4903
600479	0.4548	0.2660	0.0902	4.6758	0.9683	4.9895
002403	0.1849	0.1414	0.0418	2.0697	0.7085	2.5082
600826	0.3751	0.3929	0.0766	4.2920	0.6934	4.5214
300220	0.2985	0.0910	-0.1467	25.1713	0.5266	15.6310
300104	-0.3677	-0.6672	-0.9727	3.2944	0.3965	-2.2120
600363	0.1573	0.2709	0.0554	3.1860	0.7050	3.3673
<b>ST Companies</b>						

Code	T1	T2	T3	T4	T5	Zeta
600860	0.1126	-0.2712	0.0016	3.2187	0.6252	2.3170
002490	-0.1457	0.0342	0.0073	0.9128	0.4765	0.9214
000526	-0.5585	-0.0239	0.0220	1.0025	0.7842	0.7547
600696	0.1339	-0.1299	0.0239	3.8492	0.2153	2.5827
000595	0.0128	-0.2673	-0.0090	3.5903	0.2319	1.9975
600608	0.3596	-3.7899	0.2883	20.6771	2.4788	10.9623
600403	-0.1046	0.2574	0.0269	1.1851	0.4157	1.4503
601005	-0.0021	-0.4586	-0.2710	2.3360	0.5292	0.3920
000932	-0.2410	0.0038	0.0715	0.4053	1.0230	1.2181
000982	-0.2457	-0.1577	-0.0013	0.6168	0.2301	0.0803

## 5. Discussion

### 5.1 Discussion

In order to determine the applicability of the KMV and Zeta models in China, the default probability of listed companies should be compared with the credit rating that credit rating agencies have issued them. Credit rating is an evaluation of the borrower's creditworthiness performed by credit rating agencies. Since China's economic system is now a market economy, credit rating is more important than ever. To investors credit rating is a good indicator of the company's ability to fulfil its financial obligations, so the credit ratings given by these credit rating agencies have a strong influence on investors' decision of whether to invest or not. Good credit ratings could therefore help China attract greater foreign direct investment. In China, there are five main credit rating agencies licensed by the government, which are respectively Dagong Global Credit Rating, China Cheng Xin International Credit Rating, China Lianhe Credit Rating, Golden Credit Rating International, and Shanghai Brilliance Credit Rating & Investors Service.

According to the Credit Rating and Certification Centre of the People's Republic of China Department of Commerce Research Institute, the credit ratings of the selected listed companies can be divided into several categories. The companies' creditworthiness is mainly assessed according to the company's financial data and financial indicators, which include the company's operating turnover changes, financial debt sales ratio, financial debt degree, physical asset turnover, efficiency of investment assets, efficiency of intangible assets, current account benefit cost ratio, anomaly coefficient, residual force coefficient of payment, cost system and various asset coefficients. The corresponding credit rating is then ascertained using a proper weighting ratio. The comparison between the default probability, Z-score and credit rating of the 30 selected listed companies is shown in Table 9.

Table 9. Comparison Between Default Probability, Z-score and Credit Rating

Blue-chip Companies				Ordinary Companies			
Code	Default Probability	Z-score	Credit Rating	Code	Default Probability	Z-score	Credit Rating
600519	1.888E-60	22.4552	BBB	600000	2.9056E-10	0.1418	BBB
002302	0.0089344	2.5422	BBB	000905	0.00058159	2.8172	A
300176	9.894E-07	7.8001	BBB	600549	3.2441E-05	2.9028	A
002307	0.0210386	0.8350	CCC	603377	4.6181E-40	11.4903	BB
002081	1.939E-09	3.2750	BB	600479	1.2839E-21	4.9895	AA
600808	0.0001808	1.7804	BB	002403	9.8236E-19	2.5082	AA
000709	0.0019622	0.5040	CCC	600826	3.5418E-12	4.5214	A
601919	2.388E-05	1.0641	BB	300220	4.762E-14	15.6310	BB
601899	4.231E-07	1.7027	BBB	300104	0.00706027	-2.2120	CC
600340	0.0004569	0.9196	CCC	600363	3.2305E-08	3.3673	A
ST Companies				ST Companies			
Code	Default Probability	Z-score	Credit Rating	Code	Default Probability	Z-score	Credit Rating
600860	2.431E-10	2.3170	CCC	600608	1.6632E-17	10.9623	C
002490	0.0001318	0.9214	D	600403	2.938E-16	1.4503	CC
000526	5.669E-10	0.7547	D	601005	5.1561E-21	0.3920	D
600696	3.347E-09	2.5827	D	000932	0.00110886	1.2181	BB
000595	1.873E-05	1.9975	C	000982	0.00012644	0.0803	B

## 5.2 Advantages and Disadvantages

It is self-evident that KMV is of great importance to contemporary credit risk research. The KMV model is a default probability prediction model based on the modern option pricing theory, which is an important innovation of traditional credit risk measurement. The KMV model can take into account information in the capital market as well as quantification and analysis of credit risk for all listed companies. Since the data required by the model comes from the stock market, market information is fully utilized—leading to a better reflection of the current credit standing of listed companies. In addition, the KMV model is based on contemporary corporate finance theory and option pricing theory, so there is a strong theoretical foundation to rely on.

The KMV model has become the most important credit risk rating model in the world thanks to the strong theoretical basis and low hypothetical condition. Application of the KMV model can improve the validity of credit risk analysis of commercial banks in China, offering a useful reference to credit risk managers.

However, every model is flawed; the KMV model is no exception. First of all, the scope of application of the KMV model has certain limitations. Generally, the KMV model is more practical for listed companies than non-listed companies. Since information on listed companies is more accessible, the market value of listed companies is easier to determine. On the other hand, information on non-listed companies is not publicly disclosed. As accounting indicators are pivotal to the KMV model, it is therefore a challenge to use the model for non-listed companies. So, we need to make some adjustments to the important variables of the KMV model when we are dealing with non-listed companies.

And the expected default probability of the companies is obtained through comparative analysis, which may reduce the accuracy of calculation to a certain extent. The KMV model also assumes that the asset value of a company is subordinated to lognormal distribution, but in actual fact the asset value of a company does not necessarily conform to this characteristic. The KMV model cannot measure portfolio risk too due to the complexity and uncertainty of the market. Consequently, we cannot get the actual default correlation between two different companies.

But the combination of Copula function theory and KMV model may help us overcome this problem for now. In short, with the gradual development and perfection of China's securities market, it will be a feasible choice for banks to use stock market data to evaluate the credit standing of listed companies.

## 6. Conclusion and Recommendations

### 6.1 Conclusion

The main purposes of this paper are as follows:

- By using the share price and financial reporting information of these listed companies, we compute the distance to default and credit default probability based on the KMV model.

- By using financial statements of these listed companies, we compute the Z-score based on the Zeta Model to determine the probability of the company going bankrupt within the next two years.
- By comparing the default probability of the KMV model and the Z-score of the Zeta model with the credit rating of these listed companies, we ascertain whether application of credit risk management model in China's banks is feasible.

Having met the above objectives of the paper, the following conclusion can be made. Blue-chip companies generally have a relatively larger Z-score and a relatively smaller default probability. The Z-score of ST companies is generally less than 1.80. For companies with a high Z-score value, the default probability of the KMV model is relatively lower in general and their credit rating is generally better, i.e. class A and B. In general, for companies with a low Z-score value, the default probability of the KMV model is relatively larger in general and their credit rating is generally poorer. But in class C and D, a few companies' default probability under KMV model is very low and their Z-score is very high, i.e. 600608 and 600696. This situation may be due to insufficient sample size and list companies' wrong financial statements though they have been audited.

It is obvious that credit rating is affected by many factors, which include the credit default risk of the subject of evaluation, the ability and willingness of the economic entity to fulfil the debt and other financial obligations on time in accordance with the contract, and the technical and professional experience of the third-party credit rating agency. The process of issuing credit ratings involves a complex and structured risk assessment of credit products. The increasing complexity of investment products has only made the relationship between rating and product risk more important than ever. But the consequences of default on these complex products may be minimal since the risk of default can be dispersed. So, the default probability derived from the KMV model and the Zeta model cannot completely correspond to the entity's credit rating as these indicators are only some reference bases to help investors make an informed decision.

## *6.2 Recommendations*

In the previous study, we found that the company's credit rating, Z-score and default probability do not correspond one by one. We can try to amend the specific subjects of the financial statements. By modifying these figures, we can get effective financial results. If there are opportunities in the future, I will re-analysis credit risk and consider more comprehensive factors.

It is self-evident that the measurement of credit risk is of great importance to banks. The risk management team of banks should establish the right model where benefit is balanced against risk. Banks have the responsibility to do the following actions to minimize the size of credit risk:

- Establish appropriate risk control models that are based on the actual situation, and quantitatively and qualitatively analyze its credit risk.



- Promote the reliability of data sources in order to provide a reasonable basis for the evaluation of enterprises' credit risk.
- Maintain the independence of internal control to enhance impartiality of the evaluation results.
- Train employees regularly to strengthen their ability to review credit and to promote their awareness of the adequacy and necessity of the credit process.

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Appendices

The solution procedure of multivariate equation for Blue-chip Companies.

Equity (Call) Parameters				Estimated Values S - BSM		Solver Target and Output			S Asset Vol	Distance to Default	d <sub>1</sub>	d <sub>2</sub>	
d <sub>1</sub>	d <sub>2</sub>	N(d <sub>1</sub> )	N(d <sub>2</sub> )	PV(F)	Equity	S Volatility	Error	MV Assets					Asset Vol
					S <sup>(a)</sup>	σ <sup>(a)</sup> <sub>s</sub>	e <sup>(a)</sup>	V <sub>t</sub>	σ <sub>v</sub>	V <sub>t</sub> * σ <sub>v</sub>	(V <sub>t</sub> -F)/(V*σ <sub>v</sub> )		
16.5526724	16.3586144	16.5526724	16.3586144	37,536,736,878	1.45278E+13	0.20226036	242.7596563	914,768,107,922	0.19405808	1.77518E+11	4.9357514	16.5526724	16.3586144
2.81614184	2.36832565	2.81614184	2.36832565	10,216,570,894	67659916116	0.60796175	4.246858353	32,617,704,776	0.44781619	14606736218	1.51412657	2.81614184	2.36832565
5.23473801	4.75558192	5.23473801	4.75558192	1,406,476,693	73940988630	0.52249998	18.47055855	15,402,796,404	0.47915609	7380343645	1.8911217	5.23473801	4.75558192
2.22598018	2.03275525	2.22598018	2.03275525	13,196,304,990	17501572510	0.48938296	3.1223403	19,913,219,010	0.19322493	3847730256	1.65011483	2.22598018	2.03275525
6.1026304	5.88933595	6.1026304	5.88933595	15,788,601,076	2.53181E+11	0.29162976	27.58503278	56,724,042,230	0.21329445	12098923236	3.34703249	6.1026304	5.88933595
3.75743203	3.56667436	3.75743203	3.56667436	32,353,848,945	1.2906E+11	0.36131881	9.356856492	65,059,207,716	0.19075767	12410543174	2.56264475	3.75743203	3.56667436
2.98907266	2.88417347	2.98907266	2.88417347	124,398,316,255	1.47196E+11	0.36058862	6.550116705	169,277,267,000	0.10489918	17757046903	2.33217668	2.98907266	2.88417347
4.24453612	4.06631756	4.24453612	4.06631756	64,683,298,308	3.12748E+11	0.32810136	12.40698167	135,649,886,752	0.17821856	24175327116	2.8609407	4.24453612	4.06631756
4.97706672	4.92439205	4.97706672	4.92439205	39,142,298,895	60104539784	0.22159947	21.97054542	50,804,335,144	0.05267466	2676101141	3.95027277	4.97706672	4.92439205
3.41277871	3.31582099	3.41277871	3.31582099	259,224,587,766	3.6634E+11	0.32444902	8.718112616	359,203,701,943	0.09695771	34827569770	2.66328595	3.41277871	3.31582099

Raw Data						Model Input			Initial - Starting Values	
Code	Stock Price	Shares	ST Debt	LT Debt	Equity	Stock Volatility	USTIY	Face Value F <sub>t</sub>	Initial Asset Value	Asset Volatility
Number	P <sub>t</sub>	Q <sub>t</sub>	L <sub>t</sub>	B <sub>t</sub>	P <sub>t</sub> *Q <sub>t</sub>	√252σ <sub>it</sub>	r <sub>t</sub>	L <sub>t</sub> + 1/2B <sub>t</sub>	V <sub>t</sub> -V <sub>t</sub> <sup>(1)</sup>	σ <sub>v</sub> -σ <sub>v</sub> <sup>(1)</sup>
600519	697.49	1,256,197,800	38,574,919,400	15,570,000	876,185,403,522	0.2026	2.75%	38,582,704,400	914,768,107,922	0.19405808
002302	17.52	1,262,354,304	9,489,406,949	2,023,700,844	22,116,447,406	0.6604	2.75%	10,501,257,370	32,617,704,776	0.44781619
300176	130.1	107,280,000	1,349,783,608	191,769,592	13,957,128,000	0.5288	2.75%	1,445,668,404	15,402,796,404	0.47915609
002307	11.31	561,379,023	10,844,226,817	5,439,590,885	6,349,196,750	0.6060	2.75%	13,564,022,260	19,913,219,010	0.19322493
002081	15.32	2,643,308,689	16,022,891,319	411,323,592.75	40,495,489,115	0.2988	2.75%	16,228,553,115	56,724,042,230	0.21329445
600808	4.13	7,700,681,186	28,093,364,985	10,324,058,866	31,803,813,298	0.3902	2.75%	33,255,394,418	65,059,207,716	0.19075767
000709	3.9	10,618,607,852	113,240,573,734	29,248,245,286	41,412,570,623	0.4288	2.75%	127,864,696,377	169,277,267,000	0.10489918
601919	6.77	10,216,274,357	43,491,993,841	45,987,431,030	69,164,177,397	0.3495	2.75%	66,485,709,356	135,649,886,752	0.17821856
601899	4.59	2,303,121,889	28,793,593,015	22,878,825,317	10,571,329,471	0.2531	2.75%	40,233,005,674	50,804,335,144	0.05267466
600340	31.39	2,954,946,709	228,063,688,976	76,768,471,543	92,755,777,196	0.3755	2.75%	266,447,924,747	359,203,701,943	0.09695771

N(-d <sub>1</sub> )	KMV Default Probability	Default Probability	Recovery Given Default RGD <sub>t</sub>	Recovery Rate	Expected Loss Given Default LGD <sub>t</sub>	European Put
N(-d <sub>1</sub> )	N(-z)	N(-d <sub>2</sub> )	Vt* N(-d <sub>1</sub> )/N(-d <sub>2</sub> )	ρ <sub>t</sub> -RGD <sub>t</sub> /F	e <sup>-rt</sup> *F-RGD <sub>t</sub>	D <sub>t</sub>
7.6575E-62	3.99214E-07	1.8881E-60	37,099,841,923	0.96156665	37,536,736,877	7.08736E-50
0.00243021	0.064996871	0.0089344	8,872,210,436	0.84487125	10,216,570,894	91278932.54
8.261E-08	0.02930405	9.8938E-07	1,286,078,420	0.88960817	1,406,476,692	1391.537076
0.01300775	0.049459726	0.02103863	12,311,937,153	0.90769072	13,196,304,989	277632152.1
5.2168E-10	0.000408408	1.9388E-09	15,263,454,691	0.94053084	15,788,601,075	30.61018934
8.5833E-05	0.005193914	0.00018077	30,891,307,189	0.92891117	32,353,848,944	5848610.03
0.00139913	0.009845699	0.00196221	120,700,762,954	0.94397255	124,398,316,254	244095934.7
1.0952E-05	0.00211193	2.3881E-05	62,211,955,850	0.93571922	64,683,298,307	1544696.759
3.2278E-07	3.90311E-05	4.2312E-07	38,756,327,765	0.96329685	39,142,298,894	16561.69885
0.00032152	0.003869081	0.00045687	252,787,426,907	0.94873108	259,224,587,765	118432375.1

The solution procedure of multivariate equation for Ordinary Companies.

Raw Data						Model Input			Initial - Starting Values	
Code	Stock Price	Shares	ST Debt	LT Debt	Equity	Stock Volatility	UST1Y	Face Value $F_t$	Initial Asset Value	Asset Volatility
t	$P_t$	$Q_t$	$L_t$	$B_t$	$P_t * Q_t$	$\sqrt{252}\sigma_{i_t}$	$r_t$	$L_t + 1/2B_t$	$V_t = v^{(1)}$	$\sigma_v = \sigma^{(1)}_v$
600000	12.59	29,352,080,397	4,070,768,000,000	1,635,487,000,000	369,542,692,198	0.2302	2.7484%	4,888,511,500,000	5,258,054,192,198	0.02
000905	10.54	531,000,000	2,974,202,798	1,578,945,406	5,596,740,000	0.4636	2.7484%	3,763,675,501	9,360,415,501	0.28
600549	25.74	1,086,628,700	8,200,721,054	1,902,124,058	27,969,822,738	0.4549	2.7484%	9,151,783,083	37,121,605,821	0.34
603377	39.98	420,000,000	709,739,664	256,822,588	16,791,600,000	0.2424	2.7484%	838,150,957	17,629,750,957	0.23
600479	14.02	348,755,931	934,385,381	111,328,036	4,889,558,153	0.2272	2.7484%	990,049,399	5,879,607,552	0.19
002403	12.37	350,320,801	1,530,952,418	562,849,203	4,333,468,308	0.2005	2.7484%	1,812,377,020	6,145,845,328	0.14
600826	13.17	420,642,288	958,603,722	332,147,765	5,539,858,933	0.3112	2.7484%	1,124,677,604	6,664,536,537	0.26
300220	20.15	126,000,000	99,559,055	1,305,966	2,538,900,000	0.4474	2.7484%	100,212,038	2,639,112,038	0.43
300104	15.33	3,989,440,192	14,494,250,336	4,069,887,216	61,158,118,143	0.7298	2.7484%	16,529,193,944	77,687,312,087	0.57
600363	12.56	443,476,750	1,682,184,075	66,089,460	5,570,067,980	0.3480	2.7484%	1,715,228,805	7,285,296,785	0.27

Equity (Call) Parameters				Estimated Values S - BSM			Solver Target and Output			\$ Asset Vol	Distance to Default
$d_1$	$d_2$	$N(d_1)$	$N(d_2)$	PV(F)	Equity $S^{(n)}$	S.Volatility $\sigma^{(n)}$	Error $\epsilon^{(n)}$	MV Assets $V_t$	Asset Vol $\sigma_v$		
\$ 6.21	6.20	1	1	4,755,985,168.875	502,069,023,326	0.16942183	0.19828519438817	5,258,054,192,198	0.02	85,061,453,464	4.34
\$ 3.52	3.25	0.99979	0.999418	3,661,643,194	5,698,919,326	0.45514516	0.00066228826295	9,360,415,501	0.28	2,594,385,044	2.16
\$ 4.34	3.99	0.99999	0.999968	8,903,680,519	28,217,946,115	0.45087884	0.00015614121331	37,121,605,821	0.34	12,722,966,727	2.20
\$ 13.43	13.20	1	1	815,428,893	16,814,322,064	0.24209661	0.00000365724883	17,629,750,957	0.23	4,070,690,423	4.13
\$ 9.67	9.48	1	1	963,209,406	4,916,398,146	0.22597725	0.00005993556975	5,879,607,552	0.19	1,110,994,115	4.40
\$ 8.90	8.76	1	1	1,763,243,929	4,382,601,399	0.19829856	0.00025423665158	6,145,845,328	0.14	869,063,558	4.99
\$ 7.11	6.86	1	1	1,094,187,874	5,570,348,663	0.30946434	0.00006025077167	6,664,536,537	0.26	1,723,824,256	3.21
\$ 7.88	7.45	1	1	97,495,315	2,541,616,723	0.44696735	0.0000228752289	2,639,112,038	0.43	1,136,019,695	2.23
\$ 3.03	2.45	0.99877	0.99294	16,081,091,607	61,624,358,337	0.72339886	0.00013528620542	77,687,312,087	0.57	44,633,800,348	1.37
\$ 5.67	5.41	1	1	1,668,729,379	5,616,567,409	0.34515474	0.00013823217211	7,285,296,785	0.27	1,938,584,862	2.87

$d_1$	$d_2$	$N(-d_1)$	KMV Default Probability	Default Probability	Recovery Given Default RGDt	Recovery Rate	Expected Loss Given Default LGDt	European Put	$D_t$
$d_1$	$d_2$	$N(-d_1)$	$N(-z)$	$N(-d_2)$	$Vt * N(-d_1)/N(-d_2)$	$\rho_{t-RGD_t/F}$	$e^{-rt} * F - RGD_t$		
6.2116	6.1955	0.0000000262%	0.00%	0.0000000291%	4,744,171,222,078	97.05%	4,755,985,168,874	1,382	4,755,985,167,493
3.5249	3.2478	0.0211800911%	1.55%	0.0581586760%	3,408,854,313	90.57%	3,661,643,193	2,129,563	3,659,513,631
4.3370	3.9943	0.0007220464%	1.40%	0.0032441434%	8,262,125,960	90.28%	8,903,680,518	288,848	8,903,391,671
13.4270	13.1961	0.0000000000%	0.00%	0.0000000000%	801,558,990	95.63%	815,428,892	0	815,428,893
9.6679	9.4790	0.0000000000%	0.00%	0.0000000000%	944,770,089	95.43%	963,209,405	0	963,209,406
8.9007	8.7593	0.0000000000%	0.00%	0.0000000000%	1,735,902,221	95.78%	1,763,243,928	0	1,763,243,929
7.1146	6.8560	0.0000000001%	0.07%	0.0000000004%	1,055,867,124	93.88%	1,094,187,873	0	1,094,187,874
7.8778	7.4473	0.0000000000%	1.27%	0.0000000000%	92,331,374	92.14%	97,495,314	0	97,495,315
3.0287	2.4542	0.1227987676%	8.53%	0.7060274328%	13,512,089,957	81.75%	16,081,091,606	113,536,918	15,967,554,688
5.6716	5.4055	0.0000007072%	0.20%	0.0000032305%	1,594,768,789	92.98%	1,668,729,378	54	1,668,729,325

The solution procedure of multivariate equation for ST Companies.

Raw Data						Model Input			Initial - Starting Values	
Code	Stock Price	Shares	ST Debt	LT Debt	Equity	Stock Volatility	UST1Y	Face Value $F_t$	Initial Asset Value	Asset Volatility
Number	$P_t$	$Q_t$	$L_t$	$B_t$	$P_t * Q_t$	$\sqrt{252}\sigma_{i_t}$	$r_t$	$L_t + 1/2B_t$	$V_t = v^{(1)}$	$\sigma_v = \sigma^{(1)}_v$
600860	6.87	422,000,000	752,644,278	148,075,447	2,899,140,000	0.31055468	2.7484%	826,682,001	3,725,822,001	0.24164909
002490	4.91	797,848,400	3,531,929,198	759,540,675	3,917,435,644	0.38495789	2.7484%	3,911,699,536	7,829,135,180	0.19261997
000526	36.68	96,195,107	3,501,987,410	17,636,793	3,528,436,525	0.23465037	2.7484%	3,510,805,807	7,039,242,332	0.11761904
600696	5.86	340,565,550	501,900,192	16,575,048	1,995,714,123	0.34255648	2.7484%	510,187,715	2,505,901,838	0.27281388
000595	5.21	764,269,250	883,889,791	225,151,241	3,981,842,793	0.47435204	2.7484%	996,465,412	4,978,308,204	0.37940504
600608	7.92	328,861,441	121,210,542	4,754,040	2,604,582,613	0.37954739	2.7484%	123,587,562	2,728,170,174	0.36235369
600403	4.68	2,390,812,402	8,595,458,947	846,063,343	11,189,002,041	0.18502637	2.7484%	9,018,490,618	20,207,492,660	0.10245014
601005	2.15	8,918,602,000	4,810,947,000	3,397,548,000	19,174,994,300	0.19935767	2.7484%	6,509,721,000	25,684,715,300	0.14883101
000932	8.11	3,015,650,025	47,920,357,605	12,428,633,063	24,456,921,703	0.41180518	2.7484%	54,134,674,137	78,591,595,840	0.12814967
000982	3.5	1,805,043,279	8,469,572,905	1,773,626,618	6,317,651,477	0.36125333	2.7484%	9,356,386,213	15,674,037,690	0.14560847

Equity (Call) Parameters					Estimated Values S - BSM		Solver Target and Output			
d <sub>1</sub>	d <sub>2</sub>	N(d <sub>1</sub> )	N(d <sub>2</sub> )	PV(F)	Equity	S.Volatility	Error	MV Assets	Asset Vol	Asset Vol
					S <sup>(n)</sup>	σ <sup>(n)</sup> <sub>s</sub>	g <sup>(n)</sup>	V <sub>t</sub>	σ <sub>V</sub>	V <sub>t</sub> * σ <sub>V</sub>
6.46517567	6.22352658	6.46517567	6.22352658	804,270,858	19082692701	0.30503378	31.1611704	3,725,822,001	0.24164909	900341496.8
3.84132212	3.64870215	3.84132212	3.64870215	3,805,654,334	16188530964	0.35783958	9.817084	7,829,135,180	0.19261997	1508047755
6.20695485	6.08933581	6.20695485	6.08933581	3,415,628,735	22893348974	0.22447749	30.1226764	7,039,242,332	0.11761904	827948929.4
6.07125609	5.7984422	6.07125609	5.7984422	496,356,653	12335876419	0.33646436	26.844985	2,505,901,838	0.27281388	683644809.5
4.5020199	4.12261486	4.5020199	4.12261486	969,451,482	18415767533	0.46174528	13.1408663	4,978,308,204	0.37940504	1888795242
8.79684878	8.43449509	8.79684878	8.43449509	120,237,134	22985160958	0.37834127	61.2289491	2,728,170,174	0.36235369	988562521.2
8.19431305	8.09186291	8.19431305	8.09186291	8,774,001,580	94588502778	0.17934909	55.5586334	20,207,492,660	0.10245014	2070260385
9.48161828	9.33278727	9.48161828	9.33278727	6,333,244,082	1.84426E+11	0.19653	74.2708004	25,684,715,300	0.14883101	3822682094
3.18756213	3.05941246	3.18756213	3.05941246	52,667,096,583	89385223080	0.35915881	7.0643211	78,591,595,840	0.12814967	10071486997
3.80493989	3.65933142	3.80493989	3.65933142	9,102,736,910	26328840051	0.32982502	10.0406525	15,674,037,690	0.14560847	2282272662

Distance to Default				KMV Default Probability	Default Probability	Recovery Given Default RGDt	Recovery Rate	Expected Loss Given Default LGD <sub>t</sub>	European Put	
(V <sub>t</sub> -F <sub>t</sub> )/(V*σ <sub>v</sub> )	d <sub>1</sub>	d <sub>2</sub>	N(-d <sub>1</sub> )	N(-z)	N(-d <sub>2</sub> )	Vt* N(-d <sub>1</sub> )/N(-d <sub>2</sub> )	ρ <sub>v</sub> -RGD <sub>t</sub> /F	e <sup>-rt</sup> *F-RGD <sub>t</sub>		D <sub>t</sub>
3.22004485	6.46517567	6.22352658	5.0591E-11	0.00064085	2.4305E-10	775,522,013	0.93811407	804,270,857	0.195479	804,270,857
2.59768673	3.84132212	3.64870215	6.1187E-05	0.0046927	0.00013178	3,635,024,788	0.92926994	3,805,654,333	501525.239	3,805,152,809
4.26165963	6.20695485	6.08933581	2.7011E-10	1.0146E-05	5.669E-10	3,353,919,810	0.95531339	3,415,628,734	1.93632121	3,415,628,733
2.91922661	6.07125609	5.7984422	6.3457E-10	0.00175451	3.3467E-09	475,145,943	0.93131592	496,356,652	1.66115094	496,356,652
2.10813894	4.5020199	4.12261486	3.3655E-06	0.01750949	1.873E-05	894,546,504	0.89771957	969,451,481	18157.6189	969,433,325
2.63471713	8.79684878	8.43449509	7.0356E-19	0.00421037	1.6632E-17	115,407,190	0.9338091	120,237,133	1.9998E-09	120,237,134
5.40463515	8.19431305	8.09186291	1.2601E-16	3.247E-08	2.938E-16	8,667,368,774	0.96106645	8,774,001,579	2.5778E-06	8,774,001,580
5.01611011	9.48161828	9.33278727	1.2518E-21	2.6364E-07	5.1561E-21	6,235,945,580	0.9579436	6,333,244,082	3.2655E-11	6,333,244,082
2.42833275	3.18756213	3.05941246	0.00071739	0.00758421	0.00110886	50,845,718,943	0.93924494	52,667,096,582	58400328.4	52,608,696,255
2.76814054	3.80493989	3.65933142	7.0919E-05	0.00281886	0.00012644	8,791,662,679	0.93964299	9,102,736,909	1150923.35	9,101,585,986